

**Open book: Only Shigley's Mechanical Engineering Design textbook is allowed**  
**Scientific calculators are allowed**  
**Return the entire question booklet and the answer sheets to the instructor**  
**Show all your work for full credit and circle your answers**

**Problem 1 (60):** A schematic of a clutch-testing machine is shown. The steel shaft rotates at a constant speed  $\omega$ . An axial load  $P$  is applied to the shaft. The torque  $T$  induced by the clutch face onto the shaft is given by

$$T = \frac{fP(D + d)}{4}$$

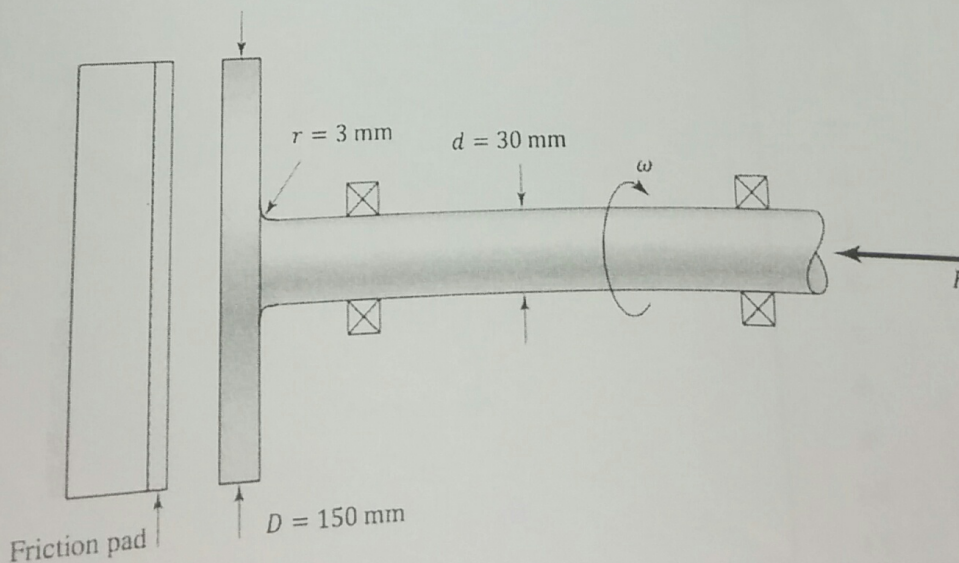
where  $D$  and  $d$  are defined in the figure and  $f = 0.3$  is the coefficient of friction of the clutch face. The theoretical stress-concentration factors for the fillet are  $K_t = 3.0$  and  $K_{ts} = 1.8$  for the axial and torsional loading, respectively.

**Static analysis:**  $P$  and  $T$  are constant static loads:

- Identify the worst location and draw a representative stress element
- Compute the nominal principal stresses, maximum shear stress, and von-Mises stress
- Choose a material for the shaft:
  - Find the maximum allowable load  $P$  such that the shaft has a factor of safety of 3 if a ductile material is used (No need to be conservative). The ductile material has  $S_y = 580$  MPa and  $S_{ut} = 690$  MPa.
  - Find the maximum allowable load  $P$  such that the shaft has a factor of safety of 3 if a brittle material is used (No need to be conservative). The brittle material has  $S_{ut} = 430$  MPa and  $S_{uc} = 1300$  MPa.
  - Which material do you recommend to use?

**Fatigue analysis:** The axial load  $P$  becomes repeated with a maximum value of  $P_{\max} = 35$  kN. Using the ductile material and the modified Goodman criteria, compute the following:

- The endurance limit
- The fatigue factor of safety
- The estimated number of cycles to failure





**Problem 2 (40):** The figure below shows the input shaft of a gearbox, supported by bearings A and B and driven by an electric motor. The tangential and radial forces experienced by the spur gear are  $F_t = 206$  N, and  $F_r = 75$  N respectively. An end-mill key-seat is used to couple the gear to the shaft. The shaft is machined from AISI 1035 CD steel. Assume 99% reliability and room temperature operation.

- Draw the force and moment diagrams for the shaft.
- For a fatigue factor of safety of 2, determine the minimum size of the shaft to endure infinite number of cycles using ASME elliptic criterion.
- From deflection consideration, is the design acceptable?

